

WJF Wiss, Janny, Elstner Associates, Inc. 330 Pfingsten Rd., Northbrook Illinois 60062	Made by: NSA	Sheet # 1/21
Morse Industries Kent, Washington	Checked by: MJS	Project #
Glass Rail Base Molding Attachment An	alysis 07/22/97	970798

Design Criteria

The purpose of these calculations is to check the adequacy of the connection of the Morse Industries glass hand railing base shoe molding (two types - see fig. 1) to either a concrete or steel substrate. The analysis considers the adequacy of the connection when when the standard height railing (42 in.) is subjected to live loads required by model building codes. The analysis is limited to the base shoe to substrate connection. Analysis of stresses in the glass, top rail, and base shoe molding are beyond the scope of these calculations.

Analysis of glass railing base shoe connections (4 types considered)

- Case 1: Concrete surface mounted (see fig. 2)
- Case 2: Concrete flush mounted (see fig. 3)
- Case 3: Steel fascia mounted (see fig. 4)
- Case 4: Steel fascia mounted (see fig. 5)

Model Code regulations require a uniform loading of 50 lbs per lineal foot (plf) or a 200-lb concentrated load to be resisted at the top rail, whichever creates the most severe stresses.

For the base shoe connection, the 200-lb load applied in a horizontal direction at the top handrail causes the maximum stresses in the connections.

The analysis considered shear and moment due to the 200 lb load being resisted by 3 - SAE Grade 5, 1/2" diameter cap screws ($F_U = 120,000 \, \text{psi}$ and $F_V = 92,000 \, \text{psi}$) and 2 - ASTM A307, 3/8" diameter T-bolts ($F_U = 60,000 \, \text{psi}$)

Reference Standards

- The Aluminum Associations (AA), *Aluminum Design Manual*, Specifications & Guidelines for Aluminum Structures, October, 1994.
- American Architectural Manufacturers Association AAMA), Metal Curtain Wall Fasteners (AAMA TIR-A9-1991), 1991
- American Concrete Institute (ACI), Building Code Requirements for Structural Concrete (ACI 318-95), 1995.
- American Institute of Steel Construction (AISC), Manual of Steel Construction (Allowable Stress Design), 9th Edition, 1989.
- Industrial Fasteners Institute (IFI), Fastener Standards, 6th Edition, 1988
- International Conference of Building Officials (ICBO), *Uniform Building Code* (UBC), Structural Engineering Design Provisions, Volume 2, 1997.
- Precast/Prestressed Concrete Institute (PCI), PSI Design Handbook, MNL 120, 4th Edition, 1992.

Note: Relevant reference to these documents in the calculations is made with [] (square brackets).





Figure 1 - 6063-T6 Aluminum Base Shoe Moldings

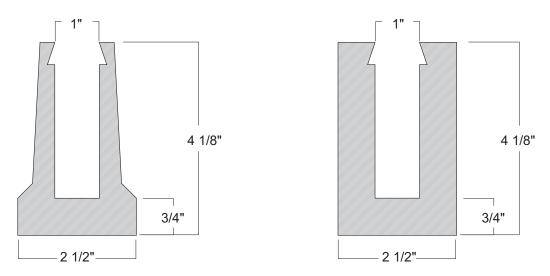
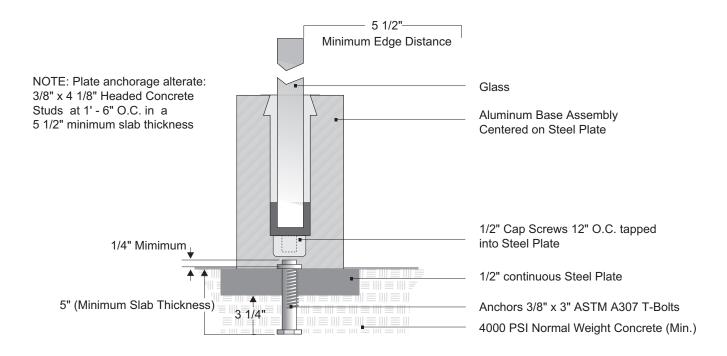


Figure 2 - Surface Mounted Base Shoe Molding





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Figure 3 - Flush Mounted Base Shoe Molding (recessed in concrete)

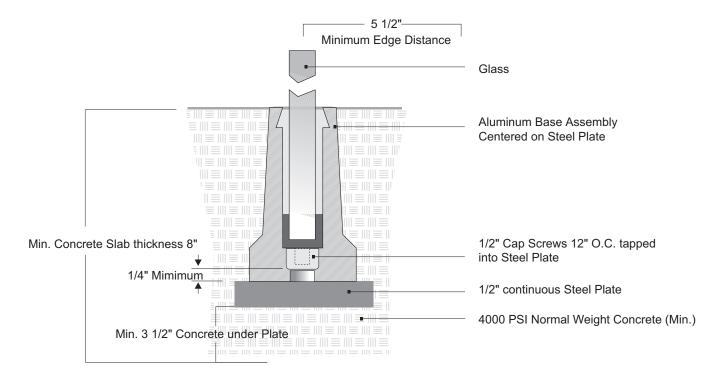
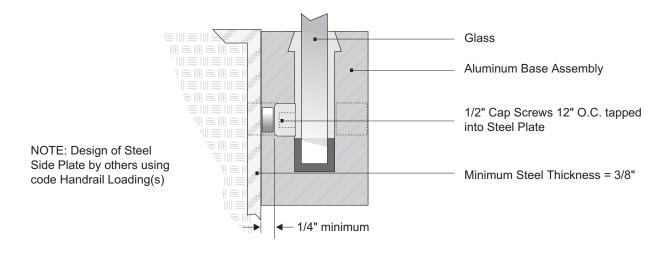


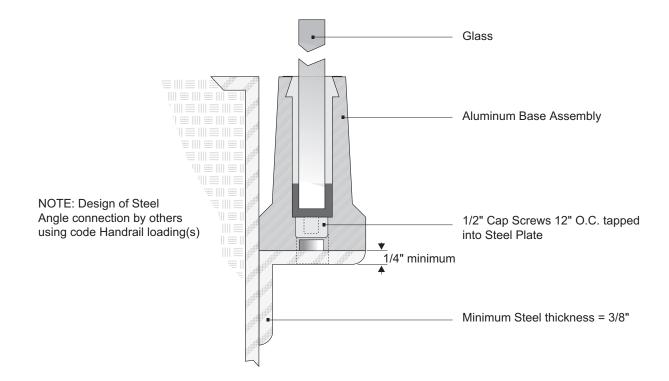
Figure 4 - Fascia Mounted Base Shoe Molding





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Figure 5 - Fascia Mounted Base Shoe Molding





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Analysis of Glass Railing Base Shoe Connections

Railing Load

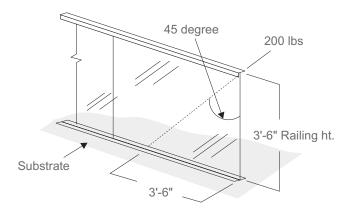
(Ref: 1997 UBC)

per Table 16-B:

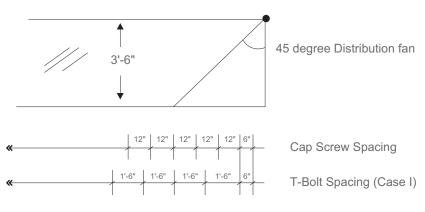
Lateral Load 50 lbs/ft

Concentrated Load 200 lbs. (not acting cumulatively with the above load)

Application



200 lbs at end of railing (into page - see above)



Maximum end distance assumed



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Material Assumptions

- Cap Screws

SAE Grade 5, 1/2" Ø Screws

F_U= 120 ksi (ultimate)

- T-Bolts F_V= 92 ksi (yield)

ASTM A307, 3/8" Ø

F_U= 60 ksi (ultimate)

- Aluminum Base Shoe Molding

Alloy 6063 -T6

- Concrete (Substrate)

F_C= 4000 psi (minimum)

- Steel (Substrate)

ASTM A36 F_V= 36 ksi (minimum)

Base Shoe Connection Types

- Case 1 Concrete surface mounted	(recessed	molding)	ļ
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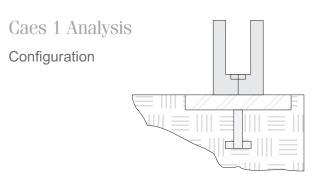
- Case 2 Concrete flush mounted (vertically attached)

- Caes 3 Steel facia mounted (horizontally attached)

- Case 4 Steel facia mounted



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1/2"Ø Cap Screws, 1'-0" o.c.

3/8" Cap Bolts, 1'-6" o.c.

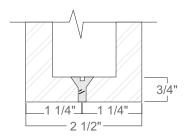
Applied Loads (Service)

Maximum at base: Shear V = 200 lbs →

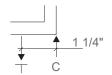
Moment M = (200 lbs)(42") = 8400 in-lbs

These loads act over a 3'-6" horizontal width, assuming a 45 degree distribution of load (page 1).

Cap Screw Connection (Screw & Aluminum checks)



Free Body Diagram



Molding assumed to be Relatively stiff

.: Arm = 1-14"

Tensile Load on One Cap Screw

M = 1.25 T

T = M/1.25 = 8400/1.25 = 6720 lbs

Conservatively, assume 3 cap screws are effective (pg 1)

6720/3 = 2240 lbs



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Tensile Allowable

 F_t = 0.33 F_u (AISC Manual of Steel Construction)

= 0.33(120 ksi) = 40 ksi

Area = $\pi d^2/4 = \pi (.5)^2/4 = 0.196$ sq. in.

T allow = $F_t A = (40 \text{ ksi})(0.196 \text{in}) = 7.84 \text{ kips} = 7840 \text{ lbs}$

7840 # >2240 lbs ok

Shear Load on Cap Screw

V = 200/3 = 66.7 lbs

Shear Allowable

 F_V = 0.17 F_U (AISC Manual - threads included)

= 0.17 (120) = 20.4 ksi

V allow = $F_V A = (20.4 \text{ ksi})(0.96 \text{ in}^2) = 3.99 \text{ kips} = 4000 \text{ lbs}$

4000 >66.7 ok

Combined

By observation → ok

Check Screw Bearing on Aluminum

Screw shank length brg on AL: 3/4" - 0.21 = 0.54 in ← Countersunk Head (Ref. IFI Stds) 3/4" - 0.5in = 0.25 in ← Socket Head

Bearing Area = $(.5)(.25 \text{ in}) = 0.125 \text{ in}^2$

Allowable bearing stress on aluminum (Aluminum Spec. '94)

Table 2-23 Fp = 24 ksi



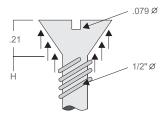
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V allow =
$$F_p A_{brg} = (24 \text{ ksi})(0.125 \text{ in}) = 3.0 \text{ kips}$$

3000 lbs >66.7 lbs ok

Check Screw Pullout in Aluminum

Countersunk Head



$$A_{p} = \pi/4 (.79^{2} - .5^{2})$$

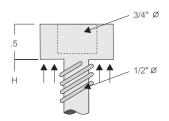
$$= 0.294 \text{ in}^{2}$$

$$A_{V} = \pi \text{dh}$$

$$= \pi(.79")(3/4" - .21)$$

$$= 1.34 \text{ in}^{2}$$

Socket Head



∼ Bearing Under Head

$$F_p$$
 = 16 ksi (conservative) on Flat surfaces \sim brg.

T allow =
$$F_pA_p$$
 = (16 ksi)(.245 in²) = 3.92 kips = 3920 lbs

>2240 lbs ok

→ Shear Plug

$$F_V = 8.5 \text{ ksi}$$
 (Aluminum Spec '94)

V allow =
$$\mathbb{F}_{U} A_{U} = (8.5 \text{ ksi})(.589 \text{ in}^2) = 5 \text{ kips}$$

>2240 lbs ok



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Cap Screw into Steel Plate

1/2" thick Steel Plate

(Ref: "Metal Curtain Wall Fasteners", from AAMA)

Table 4 Thread Stripping Area - Internal (sq. in. / thread)

$$1/2$$
"Ø TSA([) = 0.036

Number of Threads / Inch N = 13 (UNC)

Allowable Tension

Min. PL - Thickness to achieve Tension Force = Allow. Shear Stress \bullet TSA(I) \bullet (N) + N

$$MT = \frac{7840 \text{ lbs}}{(.4)(36,000)(0.86)(13)} + \frac{1}{13}$$

$$F_V = .4F_y$$

$$\frac{7840}{16099} + \frac{1}{13} = 0.56 \text{ in}$$
 1/2" PL provided

Reduction Factor = .5/.56 = 0.88

Tallow = (7840 lbs)(.88) = 6900 lbs

>2240 lbs ok

Anchor in Concrete (Steel check)

3/8" Ø A307 bolts assumed to act as studs.

Bolt Tension

4 in wide plate assume Arm = 4/2 = 2 in

On page 1, 2 stud bolts assumed effective

$$T = \frac{M}{Arm} = \frac{8400 \text{ in lbs}}{(2 \text{ in})(2 \text{ bolts})} = 2100 \text{ lbs/bolt}$$



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Allowable Tension

(Ref: AISC Manual) $F_t = 20 \text{ ksi}$

Area = $\pi(3/8")^2/4 = 0.11 \text{ in}^2$

T allow = $(20 \text{ ksi})(.11 \text{ in}^2) = 2.2 \text{ kips} = 2200 \text{ lbs}$

>2100 lbs ok

Shear in Bolt

200 lbs / 2 bolts = 100 lbs →

Allowable Shear

F_V = 10 ksi (Ref. AISC MAnual)

V allow = (10 ksi)(.11) = 1100 lbs

>100 lbs ok

Check Interaction

(AISC Table J3.3) $F_t = 26 - 1.8 F_V < 20$

 $\overline{F}_{V} = 100/.11 = 909 \text{ psi}$

Ft = 2100/.11 = 19,090 psi = 19.1 ksi

Allowable

∴ F_t = 26-1.8(0.91 ksi) = 24.36 ksi use 20 ksi as default

 $F_t > f_t$ ok



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Check Steel Plate

1/2" thick \mathbb{R} , studs at 18in oc. Assume 6" of plate is tributary to resist bending

$$s = bd^{2} = (6")(.5)^{2} = 0.25 \text{ in}^{3}$$



= 2100 lbs

$$M = (2100 lbs)(2") = 4200 in lbs$$

$$\underline{m}$$
 (4.2 in kips)
Fb = s = .25 in³ = 16.8 ksi

$$Fb = 0.75 Fy = 0.75 (36) = 27 kis$$
 ok

Check Stud in Concrete

(Ref: PCI Design Handbook, 4th edition, Chapter 6)

Factored Loads (refer to pages 6& 7)

$$V = (100 lbs)(1.7) = 170 lbs$$

 $T = (2100 lbs)(1.7) = 3570 lbs$

Bolt Geometry

As a practical minimum, select a 3" long bolt (AISC Manual) 3/8" hex head bolty F = 9/16" (dist. across flats)

Pull - Out Cone (Tension)

$$\ell e = 3 \text{ in}$$
 Ao = $\sqrt{2} \ell e \pi (\ell e = d_h)$
 $d_h = 9/16 \text{ in}$ = $\sqrt{2}(3)(\pi)[3.5625"] = 47.5 \text{ in}^2$



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F'c = 4000 psi (mimimum)

$$\ell \text{ pc} = \ell \text{ Ao } (2.8 \times \sqrt{\text{F'c}})$$

$$= (0.85) (47.5) (2.8) \sqrt{4000}$$

$$= 7150 \text{ lbs} > 3570 \text{ obs ok}$$

Shear

Min. edge distance = 15Db = 15 (3/8") = 5.625 in
$$\text{ eVc} = \text{ e628db}^2 \ \lambda \text{ fc} \ \eta \qquad \text{where} \ \eta = \text{number of studs}$$

$$= (.85) \ (628) \ (.375)^2 \ \ (1.0) \ \ \sqrt{4000} \ \ (1.0)$$

$$= 4750 \ \text{lbs} \qquad > 170 \ \text{lbs} \qquad \text{ok}$$

Examine Shear Parameters

Bolt length + PL Thickness =
$$3" + 1/2" = 3 1/2"$$

Say practical min. edge dist. = $1.5 (3.5) = 5 1/4" = de$
 $1.5 (3.5) = 1 1/4$

- * Corner Effect Cc = 1.0
 - → Keep edge distance >5 1/4" in both directions.



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$$\ell \vee_{c} = \ell \vee_{c} C_{w}C_{t} C_{c}$$

$$= (8085 lbs.) (1.0) (0.73) (1.0)$$

$$= 5092 lbs$$

Other egn still governs

(Note: A 5" min. slab thickness is a practical minimum for this ₱ & bolt combination)

Check Combined

$$Pc = 7150/.85 = 8412 lbs$$

$$Vc = 4750/.85 = 5588 lbs$$

$$\frac{1}{\ell} \left[\left(\frac{Pu}{Pc} \right)^{2} + \left(\frac{Vu}{Vc} \right) \right] \leq 1.0$$

$$\frac{1}{.85} \qquad \left[\left(\frac{3750}{8412} \right)^2 + \left(\frac{170}{5588} \right)^2 \right] \le 1.0$$

$$\frac{1}{.85}$$
 [.18 + .001] \leq 1.0

Weld bolt to plate

3/8" Ø Length =
$$2\pi_V = (3/8")(\pi) = 1.178$$

$$T = 2100 \text{ lbs } 2.1 \text{ kips}$$

V = 100 lbs = 0.1 kips

E70 electodes
$$Fv = (.3) (70 \text{ ksi}) = 21 \text{ ksi}$$

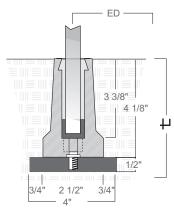
No need to check interaction as tension dominates



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Configuration

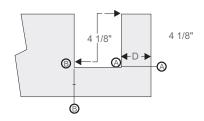


200 lbs over 42" width

$$Vu 1.7 (0.2) = 0.34 \text{ kips}$$

Evaluate a Resisting Couple in the Molding

FBD



$$N \approx M = 15.7 / 4.125 = 3.81 \text{ kips}$$

 $4 1/8"$

or

$$MA = N(4 1/8") = 15.7 in kips$$

Section A-A

Analyze as a plain concrete section

(Ref: ACI 318-95)

Section 9.3.5 ℓ = 0.65 Stregth reduction factor

Chapter 22 ~ Structural Plain Concrete

 $Mu = \ell Mn = \ell 5 \sqrt{f'c} S$ [Eq'n 22-2]



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Determine req'd section modulus ~ S

$$S = Mu$$
 15,700 in lbs (.65) (5) $\sqrt{4000}$

Determine min. width req'd

$$5 = bd_2 / 6$$
 $d = \sqrt{\frac{65}{b}} = \sqrt{\frac{6(76.4)}{42"}} = 3.3 in$

where b = 42" (effective width resisting the load, p.1)

From center of railing to edge

$$ED = 4/2 + 3.3 = 5.3$$
 in say 5 1/2" min.

∼Shear across interface

Section B-B

Slight increase in moment; the depth at B-B will be at least 3 1/2"

Arm =
$$(42" + 45/8" + 3.5/2) = 48.375$$

Mu = $(1.7) (48.375) (0.2 \text{ kips}) = 16.45 \text{ in kips}$

$$\sim$$
 Check 3 1/2 in of concrete below $\,\mathbb{R}\,$

$$S = \frac{bd_2}{6} = \frac{(42'')(3.5)_2}{6} = 85.75 \text{ in }^3$$

$$\ell$$
 Mn = ℓ 5 \sqrt{fc} S = (.65)5 $\sqrt{4000}$ (85.75) (1/1000)
= 17.63 in kips > 16.45 in kips ok



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∼Shear across section

Glass weighs 15 psf/lin thickness

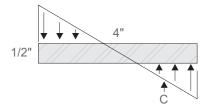
3/4" thick glass \sim w = 11.3 psf

1 ft width:

 $w = (11.3 \text{ psf}) \text{ (4 ft)} = 45.2 \text{ lbs/ft.} \\ \text{Where 4 ft height includes top hardrail wt. (approv)} \\ \text{Wu} = (1.4) \text{ (45.2/ft.)} + (1.7) \text{ (50)} = 148 \text{ lbs over 1 ft} \\ \text{Effective Width} = 3.5 \text{ ft} \\ \text{Wu} \text{ (148 lbs/ft)} \text{ (3.5 ft)} = 520 \text{ lbs} <<8.1 \text{ kips ok} \\ \end{aligned}$

Evaluate a Resisting Couple in the Steel Plate

FBD



M = 15.7 in. kips
Arms = 2/3 (4") = 2.667"
C
$$\approx 15.7 = 5.9$$
 kips
 2.667

By inspection, the concrete section (3 1/2" min.) below this has the necessary capacity to resist the moment & shear (C force) at the previously identified section B-B.

At the top, the upward reacting C force acts over an area:

$$A = (3/4") (42") = 31.5 \text{ sq. in.}$$

Check concrete bearing

$$Fp = 5900 lbs = 187 psi 31.5 in2$$

Allowable ACI 22.5.5

$$Fp = \mathbf{\ell}0.85fc = (.65)(.85)(4000psi) = 2210 psi ok$$



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Evaluate Cap Screw Fastener

Moment slightly higher M = 9225 in lbs (see page 11) T = M/1.25" = 9225/1.5 = 7380 lbs 3 cap screws effective 7380/3 = 2460 lbs

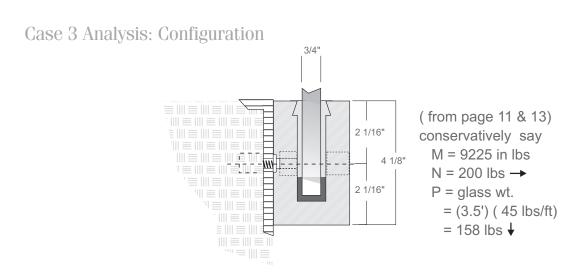
Allowables

(page 4) screw tensile allowable = 7840 lbs $\,$ ok (page 5) tensile brg under head = 3920 lbs $\,$ \rightarrow ok

: screw connection remains ok

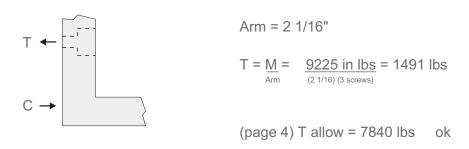


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Cap Screw Connection

Tensile Load on One Cap Screw Again, conservatively assume that 3 screws are effective



Shear Load on Cap Screw

$$V = 520/3 = 173 lbs$$



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(page 5) Brg. on aluminum with 1/4" min. V allow = 3000 lbs

ok

(page 5) Brg. on aluminum under head for tensile load T allow = 3920 lbs ok

Check Allowable Tensile Capacity into ₱ or <

(page 6) Min. Steel Thickness (MT) = 0.56"

: As a practical mimimum, use 3/8" thick steel

Check screw bearing in Steel Angle

Say
$$t = 3/8$$
" screw $\emptyset = 1/2$ "
A36 steel Fu = 58 ksi (Ref: AISC Manual)

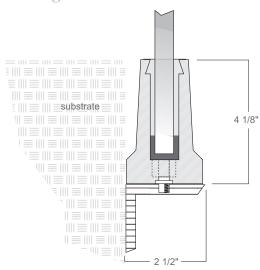
$$V_{\text{brg-allow}} = (3/8") (1/2") (1.2) (58 \text{ ksi})$$

= 13 kips ok (does not control)



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(from page 11 & 13)
M = 9225 in lbs
N = 200 lbs →
DL

P = (3.5') (45)
= 158 lbs ↓

Cap Screw Connection

Arm = (2 1/2) (1/2) = 1 1/4" Again, 3 screws effective
$$T = M + 9225 = 2460$$
 lbs $\frac{M}{Arm} = \frac{9225}{(3)(1.25)} = 2460$ lbs